

Discussion “Expectations-Driven Liquidity Traps:  
Implications for Monetary and Fiscal Policy” Nakata  
Schmidt  
SUERF Bank of Italy Conference

Discussant: Juan Passadore (EIEF)

November 2020

# Intro

- Interesting Paper. Important question. **In a nutshell:**
  - Theory: Textbook NK model. Central Bank lacks commitment.
  - **Equilibrium multiplicity.** Construct an equilibrium that switches between two states. Sunspot: No change in fundamentals, coordination failure.
  - Many results in the paper. Two of them subject to recent policy discussions:
    - Raise the inflation target?
    - Expansionary fiscal policy.
- **Discussion:**
  - Commitment.
  - Alternative explanation. Secular Stagnation: low real rates.
  - What can we learn from data?
  - Fiscal policy.

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# Policy Problem: Unconstrained

- Programming problem of Central Bank. No commitment, Markov policy problem, government optimizes given current conditions:

$$V(s) = \min_{\pi(s), y(s), i(s)} [\pi(s) - \pi^*]^2 + \bar{\lambda}y(s)^2 + \beta \mathbb{E}V(s')$$

subject to

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- Previous system pins down the allocation. **Last step.** Given  $\{\pi, y\}$  solve for  $i$ . What rate is compatible with inflation and output? Euler equation:

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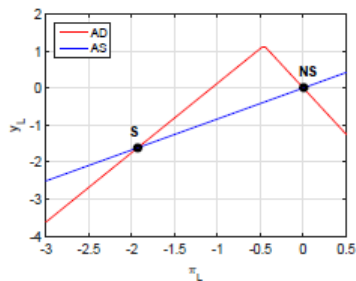
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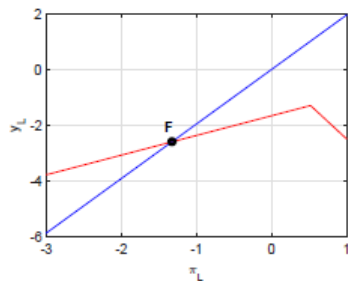
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# Sunspot vs Fundamental

Figure 1: Aggregate demand and aggregate supply in the low state



(a) Model with sunspot shock



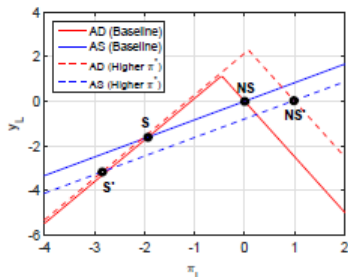
(b) Model with fundamental shock

Note: In the left panel, *S* marks low-state output gap and inflation in the sunspot equilibrium and *NS* marks low-state output gap and inflation in the no-sunspot equilibrium. In the right panel, *F* marks low-state output gap and inflation in the fundamental equilibrium. Inflation is expressed in annualized terms.

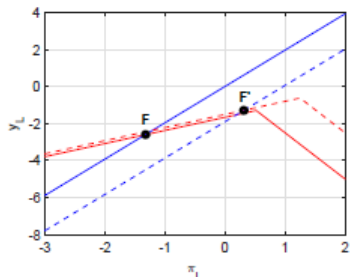


# Sunspot vs Fundamental: Raise the target? Depends...

Figure 2: The effect of increasing the central bank's inflation target



(a) Model with sunspot shock



(b) Model with fundamental shock

Note: Solid lines:  $\pi^* = 0$ ; dashed lines:  $\pi^* = 1/400$ . In the left (right) panel,  $S$  ( $F$ ) marks output gap and inflation in the sunspot (fundamental) equilibrium in the baseline and  $S'$  ( $F'$ ) marks outcomes in the sunspot (fundamental) equilibrium in the case of a higher  $\pi^*$ .  $NS$  marks output gap and inflation in the no-sunspot equilibrium in the baseline, and  $NS'$  marks outcomes in the no-sunspot equilibrium in the case of a higher  $\pi^*$ . Inflation is expressed in annualized terms.

# 1. Commitment

- Optimal policy with **commitment**. Key: **ability to make and fulfill promises**. Central Banks are currently engaged in: Forward Guidance, Unconventional monetary policy, Long run targeting...
- Some of these policies involve some degree of commitment to future policies. Why it matters? Werning (2012). NK model in a liquidity trap.
  - **Optimal policy lack of commitment**. Recession. Even Depression.
  - **Optimal policy commitment**. Optimal Policy: low rates for a long period of time. Promise a boom. Stimulates output today.
- **Question**: What do we know about the existence of the self-fulfilling liquidity trap with commitment? About the policies to mitigate this trap (fiscal and monetary)?
- **Hard problem**. **History matters**.

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- Among other reasons (for pushing real rates down)
  - large crisis and deleveraging
  - aging population
  - scarcity of safe assets
  - excess savings from corporations
  - inequality
  - downward trend in the price of capital goods
- Negative real rates: competing explanation. We need to think about both scenarios. Reality, probably a combination of both.

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  - Caramp Singh (2020), **bond premium cyclical**. Yes the US.
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  - This paper: hold on, multiplicity, contractionary.
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  - Regional multipliers. Positive, and larger in the liquidity trap. Nakamura Steinsson (2014), Sarto (2020) methodology to estimate the intercept.
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